

DIAGNOSTIC TESTS

Success in calculus depends to a large extent on knowledge of the mathematics that precedes calculus: algebra, analytic geometry, functions, and trigonometry. The following tests are intended to diagnose weaknesses that you might have in these areas. After taking each test you can check your answers against the given answers and, if necessary, refresh your skills by referring to the review materials that are provided.

A | DIAGNOSTIC TEST: ALGEBRA

1. Evaluate each expression without using a calculator.

(a) $(-3)^4$ (b) -3^4 (c) 3^{-4}

2. Simplify each expression. Write your answer without negative exponents.

$$(3a^3b^3)(4ab^2)^2$$

$$\left(\frac{3x^{3/2}y^3}{x^2y^{-1/2}}\right)^{-2}$$

3. Expand and simplify.

$$3(x + 6) + 4(2x - 5)$$

$$(\sqrt{a} + \sqrt{b})(\sqrt{a} - \sqrt{b})$$

4. Factor each expression.

$$x^4 + 27x$$

$$x^3 - 3x^2 - 4x + 12$$

5. Simplify the rational expression.

$$\frac{x^2 + 3x + 2}{x^2 - x - 2}$$

$$\frac{x^2}{x^2 - 4} - \frac{x + 1}{x + 2}$$

6. Rationalize the expression and simplify.

(a) $\frac{\sqrt{10}}{\sqrt{5} - 2}$

7. Rewrite by completing the square.

$$x^2 + x + 1$$

8. Solve the equation. (Find only the real solutions.)

$$2x^2 + 4x + 1 = 0$$

$$3|x - 4| = 10$$

9. Solve each inequality. Write your answer using interval notation.

$$-4 < 5 - 3x \leq 17$$

$$\frac{2x - 3}{x + 1} \leq 1$$

10. State whether each equation is true or false.

$$(p + q)^2 = p^2 + q^2$$

$$\frac{1 + TC}{C} = 1 + T$$